



Allowed Tables and Charts: None

Answer all the Following Questions

Question (1)

(50 Marks)

- A. Derive the Navier-Stokes equation for unsteady three-dimensional incompressible flow. Reduce the final forms to steady incompressible flow. (20 Marks)
- B. An incompressible fluid flow between two fixed parallel-horizontal plates is allowed under a constant pressure gradient ($dp/dx = \text{constant}$). Give the suitable assumptions to reduce the derived Navier-Stokes equations and derive the velocity distribution, the maximum velocity, the average velocity, the local wall shear stress and the flow rate between the plates. (20 Marks)
- C. Explain how to develop the Reynolds-stresses matrix. (10 Marks)

Question (2)

(50 Marks)

- A. Give a brief outline of the Blasius solution of laminar boundary layer for flow over a flat plate in the form: $ff'' + 2f''' = 0$. What are the boundary conditions from which the analytical solution can be developed. Write the function of the boundary layer and displacement thicknesses developing in streamwise direction. (15 Marks)
- B. Derive the growth of the turbulent boundary layer thickness, the displacement thickness, the momentum thickness and the wall skin friction coefficient of a turbulent flow over a flat plate. How do you compute the total drag force of the plate? (15 Marks)
- C. The velocity profile in a laminar boundary layer over a smooth flat plate (length L) immersed parallel to the flow stream can be approximated by a fourth degree polynomial velocity distribution as follows:

$$\frac{u}{U_{\infty}} = a + b\left(\frac{y}{\delta}\right) + c\left(\frac{y}{\delta}\right)^2 + d\left(\frac{y}{\delta}\right)^3 + e\left(\frac{y}{\delta}\right)^4$$

- (I) Compute the coefficients a, b, c, d and e. (5 Marks)
- (II) Prove the validity of the following relations: $\delta_1/\delta = 3/10$, $\theta/\delta = 37/315$, $\delta/x = 5.84/\sqrt{\text{Re}_x}$ and $C_d = 1.37/\sqrt{\text{Re}_L}$, where C_d is the drag coefficient. (5 Marks)
- D. Discuss the different regions in the boundary layer. Write the law of the wall, from which how do you derive the Clauser's plot relation? (10 Marks)

Best wishes
Assoc. Professor Wageh El-Askary