

Answer all the following questions:

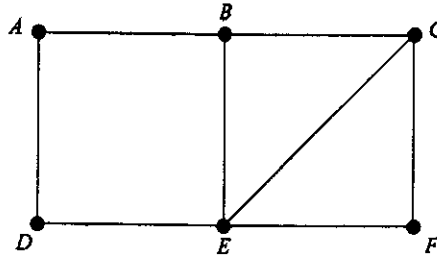
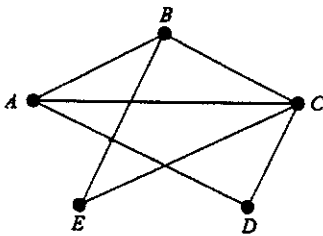
Q.1 (A) Define each of the following concepts: Directed Graph- Regular Graphs- Spanning Trees.

(B) State the difference between Relation and Function.

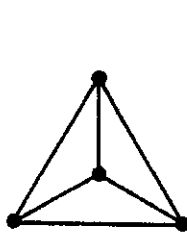
(C) Consider the following graphs

(i) Describe G formally, that is, find the set $V(G)$ of vertices of G and the set $E(G)$ of edges for each graph G .

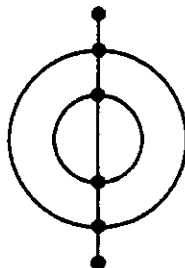
(ii) Find the degree of each vertex and verify Theorem that illustrates the relation among the vertices and edges for each graph G .



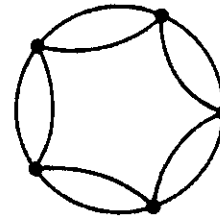
(D) Count the number V of vertices, the number E of edges, and the number R of regions of each map of the following Figures; and verify Euler's formula. Also find the degree d of the outside region



(a)

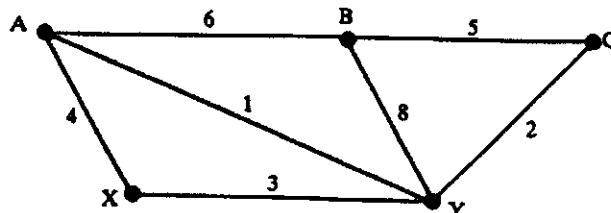


(b)



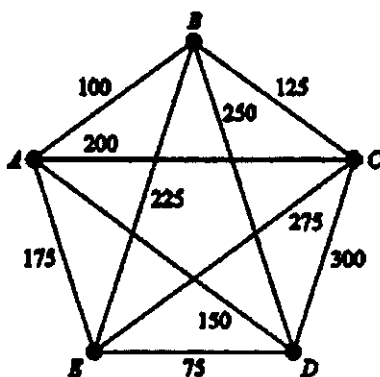
(c)

(E) Find the weight matrix $W = [w_{ij}]$ of the weighted graph G in the following Figure.



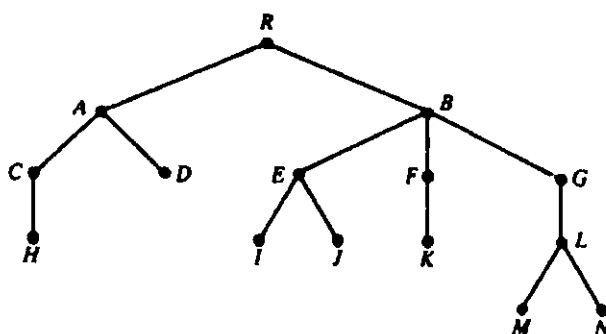
(a)

Q.2 (A) Apply the nearest-neighbor algorithm to the complete weighted graph G in Fig. (a) Beginning at: (i) vertex A ; (ii) vertex D .



(B) Let T be the rooted tree in the following Figure

- (i) Identify the path α from the root R to each of the following vertices, and find the level number n of the vertex: (i) H ; (ii) F ; (iii) M .
- (ii) Find the siblings of E .
- (iii) Find the leaves of T .



(C) Write the dual of each Boolean equation:

- (i) $(a * 1) * (0 + a') = 0$;
- (ii) $a + a'b = a + b$.

(D) Let p be "It is cold" and let q be "It is raining". Give a simple verbal sentence which describes each of the following statements: (a) $\neg p$; (b) $p \wedge q$; (c) $p \vee q$; (d) $q \vee \neg p$.

(E) Find the truth table of $\neg p \wedge q$.

(F) Consider the relation $R = \{(a, a), (a, b), (b, c), (c, c)\}$ on the set $A = \{a, b, c\}$. Find: (i) reflexive(R); (ii) symmetric(R); (iii) transitive(R).

Wish my best wishes

This document assesses the following skills:						
Question Number	Q1(1-a)	Q1(1-b)	Q1(1-c), Q3(1-g)	Q1(1-e)	Q3(1-f)	Q1(1-h)
Skills	Q2(2-a)	Q4(1-d)	Q2(2-c)	Q2(2-b)	Q4(1-e)	Q2(2-d)
	Knowledge & understanding Skills			Intellectual Skills		Professional Skills