



Allowed Tables and Charts: None

Answer all the following Questions

[100 Marks for all]

Question (1)

(50 Marks)

- (a) What are the main classifications of fluid behavior? Show different examples of Non-Newtonian fluids and plot the main flow curves indicating the various types of time-dependent fluids. (10 Marks)
- (b) Derive the velocity profile and the volume flow rate and walls shear stress of Bingham plastics-flow between two parallel plates for the following conditions:
 (I) Fixed plates (15 Marks)
 (II) Moving the upper plate with velocity U_w and fixing the lower one (15 Marks)
- (c) For Bingham plastics flow in a circular pipe, derive the Buckingham's equation and how to reduce it to Newtonian fluids. (10 Marks)

Question (2)

(50 Marks)

- (a) Develop expressions for the boundary layer thickness δ , the wall shear stress τ_w , the total frictional drag force F_{df} and the drag coefficient C_{df} for laminar boundary layer flow of power law fluids over a flat plate with zero pressure gradient flow, assuming the velocity profile in the boundary layer to be given by:

$$\frac{u}{U_x} = A + B \left(\frac{y}{\delta}\right) - C \left(\frac{y}{\delta}\right)^3 \quad (25 \text{ Marks})$$

- (b) Compare the previous results obtained in (a) if the velocity profile is expressed as:

$$\frac{u}{U_x} = C \sin\left(D \frac{y}{\delta}\right) \quad (25 \text{ Marks})$$

Best wishes

Assoc. Prof. Dr. Eng. Wageeh El-Askary

The following relations may be used:

x-Momentum:

$$\rho \left[\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right] = -\frac{\partial p}{\partial x} - \left(\frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \tau_{yx}}{\partial y} + \frac{\partial \tau_{zx}}{\partial z} \right) + \rho g_x$$

z-Momentum (cylindrical coordinates)

$$\rho \left[\frac{\partial v_z}{\partial t} + v_r \frac{\partial v_z}{\partial r} + \frac{v_\theta}{r} \frac{\partial v_z}{\partial \theta} + v_z \frac{\partial v_z}{\partial z} \right] = -\frac{\partial p}{\partial z} - \left(\frac{1}{r} \frac{\partial r \tau_{rz}}{\partial r} + \frac{1}{r} \frac{\partial \tau_{\theta z}}{\partial \theta} + \frac{\partial \tau_{zz}}{\partial z} \right) + \rho g_z$$